

LESSON-31

Mass transfer plays an important and significant role in our daily lives. Mass transfer is a phenomenon that takes place in numerous activities which we undertake during day to day working such as adding sugar to tea, adding salt in a vegetable curry, evaporation of water in to air in a cooler, drying of wet clothes, etc.

Mass transfer involves movement of matter of a substance from one place to another place. It is different from movement of bulk fluid such as air movement caused by a fan or blower and flow of water caused through a pipe due to pressure difference or by a pump. In mass transfer, movement is caused by differences in concentration of the substances between two regions. Mixing of two gases upon removal of a boundary separating them in a container is an example of mass transfer on account of concentration differences as shown in Figure 1.

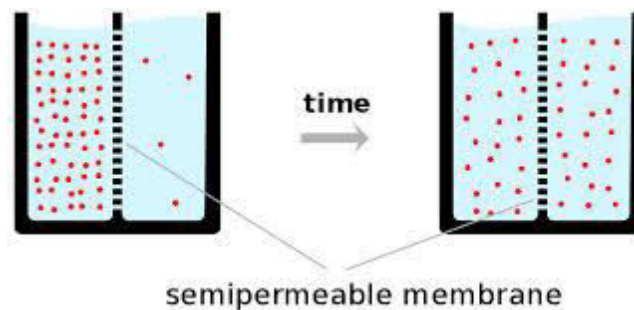


Figure 1

Concentration of a substance quantifies the amount of the substance per unit volume. This amount can be on a mass or molar basis. The mass concentration of a particular substance called the density and is expressed as

$$\rho_k = \frac{m_k}{V} \quad (1)$$

In mass transfer concentration means molar concentration and is expressed as

$$C_k = \frac{n_k}{V} \quad (2)$$

In mass transfer, movement of a matter of substance occurs due to concentration gradient and movement is always from high concentration region to low concentration region. The mass transfer will continue till the concentration differences between two regions exist and will stop when equilibrium is obtained. Mass transfer basically deals with transport of species:

- **within a medium** for example sugar dissolves in a cup of tea to sweeten the entire tea cup as shown in Figure 2.

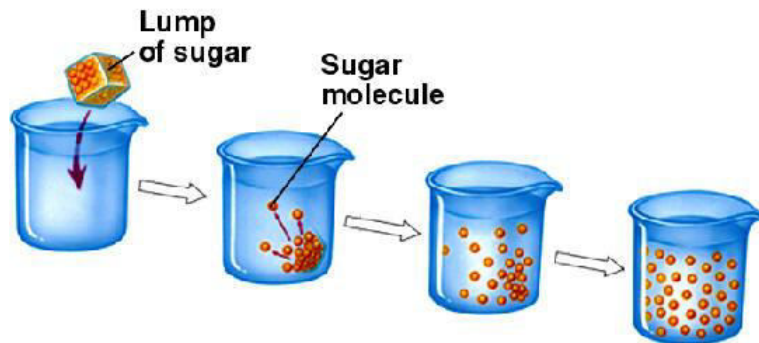


Figure 2

- **across an interface** for example from one medium to another i.e. spreading of food odour in the entire house as shown in Figure 3.

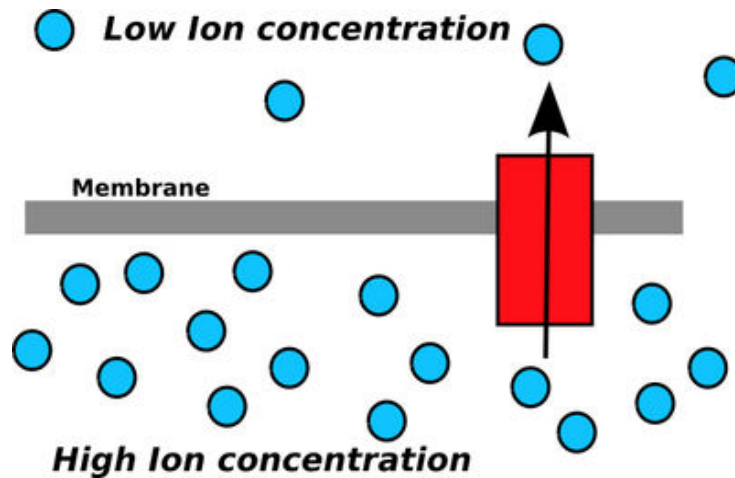


Figure 3

Mass transfer is similar to heat transfer in following ways:

- The driving force for heat transfer is temperature gradient whereas mass transfer occurs due to concentration gradient.
- Heat transfer always takes place from high to low temperature regions, similarly mass is transferred towards low concentration regions, thereby, decreasing the temperature gradient.
- Heat transfer stops immediately when temperature difference becomes zero, similarly, mass transfer ceases when concentration gradient is reduced to zero.
- The rates of heat and mass transfer depend upon the driving potential and resistance.

Types of Mass Transfer:

Transfer of mass takes place under different conditions and depending upon the conditions, it can be classified into different categories which are shown in Figure 4.

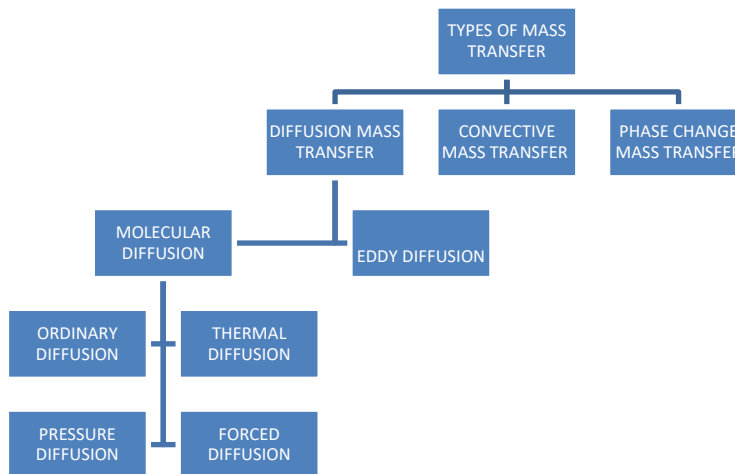


Figure 4

1. **Diffusion Mass Transfer:** Diffusion mass transfer can be classified into two categories:
 - i) **Molecular Mass Diffusion:** This type of mass transfer occurs at a macroscopic level in which transfer of mass takes place from a region of high concentration to low concentration in a mixture of liquids or gases. Transfer of mass by diffusion occurs due to
 - **Presence of concentration gradient** in a mixture and is called ordinary diffusion as shown in Figure 5.

Diffusion

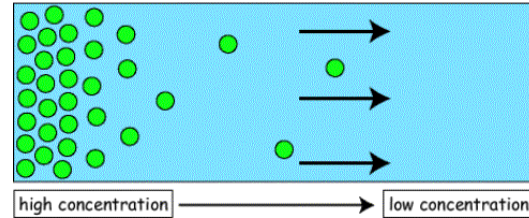


Figure 5

- **Presence of thermal gradient** and is termed as thermal diffusion
 - **Presence of pressure gradient** and is termed as pressure diffusion
 - **Presence of external forces** and is termed as forced diffusion
- ii) **Eddy Diffusion:** Mass transfer by eddy diffusion occurs when one of the diffusing fluids is in turbulent motion and is in addition to the diffusion mass transfer. The turbulent motion increases mass transfer.
2. **Convective Mass Transfer:** Mass transfer occurring between a moving fluid and a surface or between two relatively immiscible fluids is termed as convective mass transfer.
3. **Mass Transfer by Phase Change:** This type of mass transfer occurs due to change in the phase of a substance.

Fick's Law of Diffusion:

The diffusion process is governed by mass transfer laws which are very similar to heat transfer laws and govern the relationship between mass flux and concentration gradient. The **basic law of diffusion** was proposed in 1855 by **Adolf Fick** which is expressed as

$$\text{Mass Flux} = \text{Constant of Proportionality} \times \text{Concentration Gradient} \quad (1)$$

Consider a system in which a partition separates two gases B and C and the two gases are maintained at same temperature and pressure initially as shown in Figure 6.

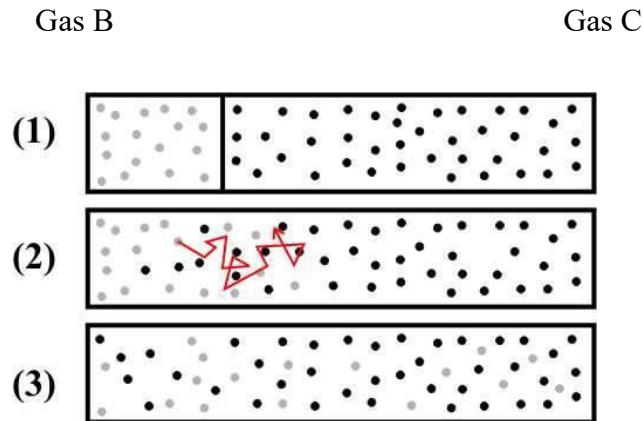


Figure 6

On removal of the partition, molecules of gas B move towards right where concentration is low while molecules of gas C move towards low concentration area i.e towards left. The molecules of both the gases diffuse with each other gradually. The diffusion rate is given by Fick's law and is expressed as

$$\frac{m_b}{A} = -D_{bc} \frac{dC_b}{dx} \quad (2)$$

m_b/A is **Mass flux or mass flow per unit area**, $\text{Kg}_m / \text{hr}\cdot\text{m}^2$

A is area through which mass is flowing, m^2

C_b is **mass concentration** or **molecules per unit volume**, kg/m^3

$\frac{dC_b}{dx}$ is **concentration gradient** for gas B

D_{bc} is the **diffusion coefficient or mass diffusivity**, m^2/Sec

The unit of diffusion coefficient or mass diffusivity is same as the units of thermal diffusivity and kinematic viscosity which is also called momentum diffusivity. Diffusion coefficients are generally determined experimentally and increase with increase in temperature but decrease with increase in pressure.

Mass flux for gas C can be expressed as

$$\frac{m_c}{A} = -D_{cb} \frac{dC_c}{dx} \quad (3)$$

By using characteristic gas equation, Fick's Law can be expressed in terms of partial pressure.

$$p_b = \rho_b R_b T = \rho_b \frac{G}{M_b} T \quad (4)$$

$$\therefore \rho_b = p_b \frac{M_b}{GT} \quad (5)$$

Density ρ_b represents mass concentration to be used in Fick's Law. Therefore,

$$\therefore \rho_b = p_b \frac{M_b}{GT} = C_b \quad (6)$$

Substituting the value of C_b from equation (6) in to equations (2) and (3), we get

$$\frac{m_b}{A} = -D_{bc} \frac{M_b}{GT} \frac{dp_b}{dx} \quad (7)$$

$$\frac{m_c}{A} = -D_{cb} \frac{M_c}{GT} \frac{dp_c}{dx} \quad (8)$$

The above equations hold good for isothermal diffusion only.

The Fick's law of diffusion as given by equations (2) and (3) is similar to Fourier's law of heat conduction and Newton's law of viscosity expressed by equations (9) and (10) respectively.

$$\frac{Q}{A} = -K \frac{dT}{dx} \quad (9)$$

$$\tau = -\mu \frac{du}{dy} \quad (10)$$

Analogy between mass, heat and momentum transfer has been shown in Table 1

Table 1:

Transport Phenomenon	Governing Law	Driving Potential
Mass Transfer	Fick's Law of Diffusion	Concentration Gradient, $\frac{dC_b}{dx}$
Heat Transfer	Fourier's law of conduction	Temperature Gradient, $\frac{dT}{dx}$
Momentum Transfer	Newton's Law of Viscosity	Velocity Gradient, $\frac{du}{dy}$

Some important aspects of Fick's law of diffusion are summarized below;

- i. Fick's law is applicable for all matter irrespective of its state: solid, liquid or gas. Mass transfer is inversely proportional to molecular spacing.
- ii. Similar to heat transfer which occurs in direction of decreasing temperature, mass transfer by diffusion also occurs in the direction of decreasing concentration.
- iii. Apart from concentration gradient, mass transfer can occur due to presence of temperature gradient, pressure gradient or external force. However, Fick's law gives rate of mass transfer on account of concentration gradient only and effect of other parameters is considered to be small or negligible.
- iv. Diffusion coefficients in gases are highest, followed by liquids and solids.
- v. Diffusion coefficient or mass diffusivity is a function of temperature, pressure and composition of a system. However, for ideal gases and dilute liquids, diffusion coefficient depends on temperature and pressure and is independent of system composition.

REVIEW QUESTIONS:

Q.1 Molecular mass diffusion occurs due to presence of

- | | |
|-------------------------|---------------------------|
| a) Thermal gradient | b) Concentration gradient |
| c) Pressure gradient | d) External forces |
| e) All the above | |

Q.2 Identify a possible case of mass transfer

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|-------------------------------------|------------------------------|
| a) Fan blowing air | b) Flow of water from height |
| c) Addition of salt in water | d) All above |

Q.3 Mass transfer is governed by

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|----------------------|----------------------|
| a) Fick's law | b) Fourier's law |
| c) Newton's law | d) None of the above |

Q.4 Diffusion coefficient generally depends upon

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|--------------------------|-------------------------|
| a) Temperature of system | b) Pressure of system |
| c) Composition of system | d) All the above |

